# Control and Higher Order Functions 2

## COMPUTER SCIENCE 61A

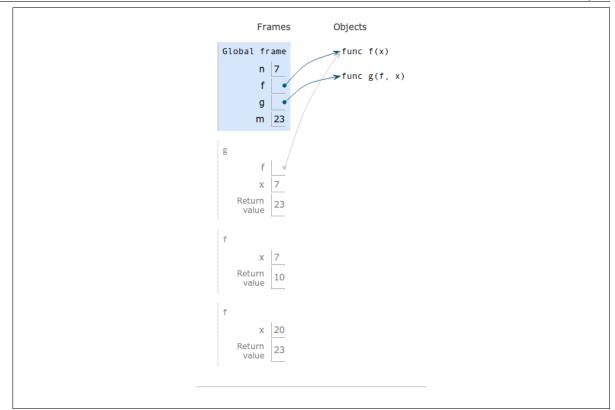
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**1** Warmup Question

1. Draw the environment diagram for this code

```
n = 7
def f(x):
    return x + 3
def g(f, x):
    return f(f(x) * 2)
m = g(f, n)
```

Solution:



Control refers to directing the computer to selectively choose which lines of code get executed

## 2.1 Conditional Statements

Conditional statements allow programs to execute different lines of code depending on the current state. A typical if-else set of statements will have the following structure:

```
if <conditional expression>:
        <suite of statements>
elif <conditional expression>:
        <suite of statements>
else:
        <suite of statements>
```

The else and elif statements are optional and you can have any number of elif statements. Here a conditional clause is something that evaluates to either True or False. The body of statements that get executed are the ones under the first true conditional clause. After a true conditional clause is found, the rest are skipped. Note that in python everything evaluates to True except False, 0, "", and None. There are other things that evaluate to False but we haven't learned them yet.

```
>>> if 2 + 3:
... print(6)
6
```

Here's some example code

```
>>> def mystery(x):
... if x > 0:
... print(x)
... else:
... x(mystery)
...
>>> mystery(5)
5
>>> mystery(-1)
TypeError: 'int' object is not callable
```

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DISCUSSION 2: CONTROL AND HIGHER ORDER FUNCTIONS

1. Write a simple function that takes in one input x, whose value is guaranteed to be between 0 and 100. if x > 75 then print "Q1". If  $50 \le x < 75$  then print "Q2". If  $25 \le xs < 50$  then print "Q3". If x < 25 then print "Q4".

```
def find_quartile(x):
```

#### Solution:

```
if x > 75:
    print("Q1")
if x > 50:
    print("Q2")
if x > 25:
    print("Q3")
else:
    print("Q4")
```

2. Now try rewriting the function so that at most 4 lines of code inside the function will ever get executed.

def find\_quartile(x):

```
Solution:
```

```
if x > 50:
    if x > 75:
        print("Q1")
    else:
        print("Q2")
elif x > 25:
        print("Q3")
else:
        print("Q4")
```

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Using conditional statements we can ignore statements. On the other hand using iteration we can repeat statements multiple times. A common iterative block of code is the while statement. The structure is as follows:

This block of code literally means while the conditional clause evaluates to True, execute the body of statements over and over.

```
>>> def countdown(x):
... while x > 0:
... print(x)
... x = x - 1
... print("Blastoff!")
...
>>> countdown(3)
3
2
1
Blastoff!
```

DISCUSSION 2: CONTROL AND HIGHER ORDER FUNCTIONS

1. Fill in the *is\_prime* function to return True if n is a prime and False otherwise. Hint: use the % operator. x%y returns the remainder when x is divided by y.

```
def is_prime(n):
```

#### Solution:

k = 2
while k < n:
 if n % k == 0:
 return False
 k += 1
return True</pre>

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	3	Functions

A function that manipulates other functions as data is called a *higher order function* (HOF). For instance, a HOF can be a function that takes functions as arguments, returns a function as its value, or both.

### 3.1 Functions as Argument Values

Suppose we would like to square or double every natural number from 1 to n and print the result as we go. Using the functions square and double, each of which are functions that take one argument that do as their name imply, fill out the following:

```
def square_every_number(n):
```

```
Solution:
```

```
i = 1
while i <= n:
    print(square(i))
    i += 1</pre>
```

def double\_every\_number(n):

#### Solution:

i = 1
while i <= n:
 print(double(i))
 i += 1</pre>

Note that the only thing different about square\_every\_number and double\_every\_number is just what function we call on n when we print it. Wouldn't it be nice to generalize functions of this form into something more convenient? When we pass in the number, couldn't we specify, also, what we want to do to each number < n.

To do that, we can define a higher order function called every. every takes in the function you want to apply to each element as an argument, and applies it to *n* natural numbers starting from 1. So to write square\_every\_number, we can simply do:

```
def square_every_number(n):
    every(square, n)
```

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```
def double_every_number(n):
    every(double, n)
```

*Note*: These functions are not pure — as defined below, every will actually print values to the screen.

## 3.2 Questions

1. Now implement the function every that takes in a function func and a number n, and applies that function to the first *n* numbers from 1 and prints the result along the way:

```
def every(func, n):
```

```
Solution:
```

i = 1
while i <= n:
 print(func(i))
 i += 1</pre>

2. Similarly, implement the function keep, which takes in a function condition cond and a number n, and only prints a number from 1 to n to the screen if it fulfills the condition:

```
def keep(cond, n):
```

## Solution:

```
i = 1
while i <= n:
    if cond(i):
        print(i)
        i += 1</pre>
```

## 3.3 Functions as Return Values

This problem comes up often: write a function that, given something, **returns a function** that does something else. The key message — conveniently emphasized — is that your

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DISCUSSION 2: CONTROL AND HIGHER ORDER FUNCTIONS

function is supposed to return a function. For now, we can do so by defining an internal function within our function definition and then returning the internal function.

That is the common form for such problems but we will learn another way to do this shortly.

- 1. Write a function and\_add\_one that takes a function f as an argument (such that f is a function of one argument). It should return a function that takes one argument, and does the same thing as f, except adds one to the result.

```
def and_add_one(f):
```

## Solution: def foo(x): return f(x) + 1 return foo

2. Write a function and\_add that takes a function f and a number n as arguments. It should return a function that takes one argument, and does the same thing as the function argument, except adds *n* to the result.

```
def and_add(f, n):
```

```
Solution:
```

```
def foo(x):
    return f(x) + n
return foo
```

3. The following code has been loaded into the python interpreter:

```
def skipped(f):
    def g():
        return f
    return g
def composed(f, g):
    def h(x):
        return f(g(x))
    return h
def added(f, g):
    def h(x):
        return f(x) + g(x)
    return h
```

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```
def square(x):
    return x*x
def two(x):
    return 2
```

What will python output when the following lines are evaluated?

```
>>> composed(square, two)(7)
```

## Solution:

4

>>> skipped(added(square, two))()(3)

## Solution:

11

```
>>> composed(two, square)(2)
```

Solution	
2	

4. Draw the environment diagram for this.

```
>>> from operator import add
>>> def curry2(h):
... def f(x):
... def g(y):
... return h(x,y)
... return g
... return f
>>> make_adder = curry2(add)
>>> add_three = make_adder(3)
>>> five = add_three(2)
```

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