## Lecture \#4: Control

- The expressions we've dealt with recently evaluate all of their operands in order.
- While there are very clever ways to do everything with just this [challenge!], it's generally clearer to introduce constructs that control the order in which their components execute.
- A control expression evaluates some or all of its operands in an order depending on the kind of expression, and typically on the values of those operands.
- A statement is a construct that produces no value (not even None, but is used solely for its side effects.
- A control statement is a statement that, like a control expression, evaluates some or all of its components, in an order that may depend on the these components.
- We typically speak of statements being executed rather than evaluated, but the two concepts are essentially the same, apart from the question of a value.


## Conditional Expressions (I)

- The most common kind of control is conditional evalutation (execution).
- In Python, to evaluate

TruePart if Condition else FalsePart

- First evaluate Condition.
- If the result is a "true value," evaluate TruePart; its value is then the value of the whole expression.
- Otherwise, evaluate FalsePart; its value is then the value of the whole expression.
- Example:

| If $x$ is $2:$ | If $x$ is $0:$ |
| :--- | :--- |
| $1 / \times$ if $x!=0$ else 1 | $1 / \times$ if $x!=0$ else 1 |
| $1 / x$ if $2!=0$ else 1 | $1 / \times$ if $0!=0$ else 1 |
| $\Longrightarrow 1 / \times$ if True else 1 | $\Longrightarrow 1 / x$ if False else 1 |
| $\Longrightarrow 1 / x$ | $\Longrightarrow 1$ |
| $\Longrightarrow 1 / 2$ | $\Longrightarrow 1$ |
| $\Longrightarrow 0.5$ |  |

## "True Values"

- Conditions in conditional constructs can have any value, not just True or False.
- For convenience, Python treats a number of values as indicating "false":
- False
- None
- 0
- Empty strings, sets, lists, tuples, and dictionaries.
- All else is a "true value" by default.
- So, for example: 13 if 0 else 5 and 13 if [] else 5 both evaluate to 5.


## Conditional Expressions (II)

- To evaluate

Left and Right

- Evaluate Left.
- If it is a false value, that becomes the value of the whole expression.
- Otherwise the value of the expression is that of Right.
- This is an example of something called "short-circuit evaluation."
- For example,
$\square$
0 and print(6) $\Longrightarrow \square$ + side-effects:
[] and $1 / 0 \Longrightarrow \square$.


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0 and print(6) $\Longrightarrow 0+$ side-effects: None.
[] and $1 / 0 \Longrightarrow[]$.

## Conditional Expressions (III)

- To evaluate

Left or Right

- Evaluate Left.
- If it is a true value, that becomes the value of the whole expression.
- Otherwise the value of the expression is that of Right.
- Another example of "short-circuit evaluation."
- For example, 5 or "Hello" $\Longrightarrow \square$. 2 or $\operatorname{print}(6) \Longrightarrow \square$ + side-effects:
[] or $1 / 0 \Longrightarrow \square$.


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- For example,

5 or "Hello" $\Longrightarrow 5$.
2 or $\operatorname{print}(6) \Longrightarrow 2$ + side-effects: None.
[] or $1 / 0 \Longrightarrow$ error.

## Chained Comparisons

- An interesting feature of Python (quite rare; Cobol has something like it) involves the relational operators:

$$
==!=\langle \rangle<=>=\text { is is not in not in }
$$

- Ordinarily, $3<4$ yields True and $4<3$ yields False.
- But what does $4>=3>1$ produce? In Java, it's an error, and in $C$, it doesn't do what you probably want.
- In Python, it's a special control expression and works as expected.
- To evaluate First > Second >= Third, for example,
- Evaluate First and Second.
- If the first value is not larger than the second, stop and yield False for the entire expression.
- Otherwise, compute the value of Third and compare against the value previously computed for Second, and yield True or False as appropriate.
- In any case, no expression is evaluated more than once.


## Chained Comparisons (II)

- So what is

$$
\text { (print("A") or } 3)<(\text { print ("B") or } 2)<(\text { print ("C") or } 4)
$$ and what does it print?

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\text { (print("A") or } 3)<(\text { print ("B") or } 2)<(\text { print ("C") or } 4)
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and what does it print?

- Prints $A$ and $B$, evaluates to False.


## Conditional Statement

- Finally, this all comes in statement form:
if Condition1:
Statements1
elif Condition2:
Statements2
else:
Statementsn
- Execute (only) Statements1 if Condition1 evaluates to a true value.
- Otherwise execute Statements2 if Condition2 evaluates to a true value (optional part).
- ...
- Otherwise execute Statementsn (optional part).


## Example

```
def signum(x):
    if x > 0:
        return 1
    elif x == 0:
        return 0
    else:
        return -1
```


## A Puzzle: Define compare3

```
# What goes here?
from operator import lt, gt # Comparison functions
gt(gt(3,2), 1) # Yields False, not like 3>2>1 (why?)
compare3(gt)(3)(2)(1) # This should yield True
compare3(gt)(3)(2)(4) # This should yield False
compare3(lt)(1)(2)(3) # This should yield True
# etc.
```


## Some Solutions

```
def compare3(op):
    def f(a):
            def g(b):
                return lambda c: op(a,b) and op(b, c)
            return g
    return f
def compare3(op):
    def f(a):
        def g(b):
            if op(a,b):
                return lambda c: op(b, c)
            else:
                        return lambda c: False
        return g
    return f
```


## Indefinite Repetition

- With conditionals and function calls, we can conduct computations of any length.
- For example, to sum the squares of all numbers from 1 to $N$ (a parameter):

```
def sum_squares(N):
    """The sum of K**2 for K from 1 to N (inclusive)."""
    if N < 1:
        return 0
    else:
        return N**2 + sum_squares(N - 1)
```

- This will repeatedly call sum_squares with decreasing values (down to 1), adding in squares:

```
sum_squares (3) => \(3 * * 2+\) sum_squares (2)
    \(\Rightarrow 3 * * 2+(2 * * 2+\) sum_squares (1))
    \(\Rightarrow 3 * * 2+(2 * * 2+(1 * * 2+\) sum_squares \((0)))\)
    \(\Rightarrow 3 * * 2+(2 * * 2+(1 * * 2+0))=>14\)
```


## Explicit Repetition

- But in the Python, C, Java, and Fortran communities, it is more usual to be explicit about the repetition.
- The simplest form is while
while Condition:
Statements
means "If condition evaluates to a true value, execute statements and repeat the entire process. Otherwise, do nothing."
- So our sum-of-squares becomes:

```
def sum_squares(N):
    """The sum of K**2 for K from 1 to N (inclusive)."""
    result = 0
    while N >= 1:
        result += N**2 # Or result = result + N**2
        N -= 1 # Or N = N-1
```

    return result
    - (Actually, this isn't quite right. What's different from the first version?)


## Going Backwards

- OK: I cheated. In the recursive version, you actually add up the squares starting from the small end.
- So to be true to the original, I would write:

```
def sum_squares(N):
    """The sum of K**2 for K from 1 to N (inclusive)."""
    result = 0
    k = 1
    while k <= N:
        result += k**2
        k += 1
    return result
```


## Definite Repetition

- In most programming languages, we write "counting loops" like the preceding with a specialized kind of loop. In Python:

```
def sum_squares(N):
    """The sum of K**2 for K from 1 to N (inclusive)."""
    result = 0
    # Original:
    # k = 1
    # while k <= N:
    # result += k**2
    # k += 1
    for k in range(1, N+1):
        result += k**2
    return result
```

- This actually means "execute result $+=\mathrm{k} * * 2$ for every value of $k$ in the range 1 (inclusive) to $\mathrm{N}+1$ (exclusive)."
- Special case of a more general version that we'll see later.

