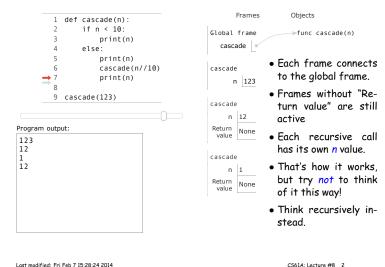
Lecture #8: More Recursion

Announcements:

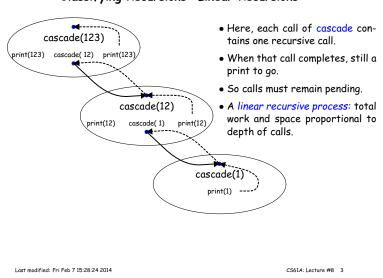
- Project #1 due next Thursday (13 Feb).
- Test #1 Tuesday, 18 Feb at 8PM.
- AWE 61A Party this Sunday (9 Feb) in the Woz, 1-3PM.
- Guerilla Sections this weekend (see Piazza).
- Self-assessment quiz will be released tonight, due Monday. Watch the website and Piazza.

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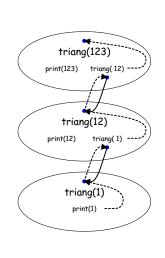
A Simple Recursion



Classifying Recursions: Linear Recursions



Classifying Recursions: Iterative Processes



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2 + 4 = 6

- def triang(n):
 print(n)
 if n < 10: triang(n-1)</pre>
- Again, each call of triang contains one recursive call.
- So this is a type of linear recursive process.
- But there's no more to do when that call completes (tail recursive)
- So in principle, calls need not remain pending.
- An iterative process: total work still proportional to depth of calls, but total space need not be.
- This kind is suitable for a loop.

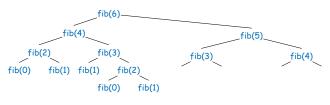
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Classifying Recursion: Tree Recursions

 Previously, we looked at a program for computing values in the Fibonacci sequence:

```
def fib(n):
    """The Nth Fibonacci number, N>=0."""
    assert n >= 0
    if n <= 1:
        return n
    else:
        return fib(n-2) + fib(n-1)</pre>
```

Here, each invocation of fib makes two calls: work is exponential in depth of calls: A $tree-recursive\ process$.



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A Tree Recursion: Partitions

- partitions(n, k): The number of non-decreasing sequences of two or more positive integers between 1 and k that add up to n.
- For example, partitions(6, 4) is 9:

```
1 + 1 + 4 = 6

3 + 3 = 6

1 + 2 + 3 = 6

1 + 1 + 1 + 3 = 6

2 + 2 + 2 = 6

1 + 1 + 2 + 2 = 6

1 + 1 + 1 + 1 + 1 + 2 = 6

1 + 1 + 1 + 1 + 1 + 1 = 6
```

Partitions, concluded This leads to the following program: def partitions(n, k): """The number of ways of partitioning N items into partitions of si <=K.""" if n == 0: return 1 elif n < 0 or k <= 0: return 0 with_k = partitions(n-k, k) without_k = partitions(n, k-1) return with_k + without_k Last modified: Fri Feb 7 15:28:24 2014 CS61A: Lecture #8 8