Lecture 32: Declarative Programming (Under	the Hood)	Review: A "Schemish" Prolog	
		 Programs in our language define subsets of Scheme express will be considered "true." 	sions that
		(fact CONCLUSION) means that CONCLUSION is to be true, for any replacement of its logical variables.	e taken as
		(fact CONCLUSION HYPOTHESIS) means that CON is to be taken as true for all replacements of the logical that cause each of the the HYPOTHESES to be true.	CLUSION variables
		<i>logical variables,</i> represented as symbols starting with '?', operands that may be replaced by other expressions (includ logical variables).	stand for ding other
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Another Example: Lists		Applying append	-to-form
 In ordinary Scheme, append (or extend in Python) is a functing two lists and returning a list. In our Scheme Prolog, it is a <i>relation between three lists</i>, we define by writing two facts about it that cover all cases: ;;; (append-to-form A B C) means "appending list B t;;; list C. ; Fact about the empty list. (fact (append-to-form () ?x ?x)) ; Fact about a general non-empty list (fact (append-to-form (?a . ?r) ?b (?a . ?s)) ; ass (append-to-form ?r ?b ?s)) 	ion tak- hich we to list A produce:	<pre>logic> (fact (append-to-form () ?x logic> (fact (append-to-form (?a .</pre>	<pre>?x)) ?r) ?b (?a . ?s)) ?s)) c) (d e f) (a b c d e f))) c) (d e f) ?x)) d e f) (a b c d e f))) c) ?y (a b c d e f))) ?r) ?x (a b c d e f)))</pre>
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Permutations (Anagrams)		Operational and Declarative Meanings	
• When is list B a permutation (reordering) of A?		• An assertion	
• An obvious fact:		(fact (eats ?P ?F) (hungry ?P) (has ?P ?F) (likes ?P ?F	·))
<pre>logic> (fact (permutation () ()))</pre>		means that for any replacement of ?P (e.g., 'brian') and ?F (e.g., 'pot stickers') throughout the rule:	;-
• Key fact: every permutation of $(a \ R)$ consists of a per of R with a inserted somewhere in that permutation:	mutation	Declarative Meaning If brian is hungry and has potstickers an	d
$(0\ 1\ 2\ 3\ 4) \implies (4\ 3\ 1\ 2)$		Operational Meaning To show that brian will eat potstickers show that brian is hungry, then that brian has potstickers, an	s, d
• Or, in our logic language:		then that brian likes potstickers.	
logic> (fact (permutation (?a . ?r) ?s) (permutation ?r ?t) (insert ?a ?t ?s)))	 The declarative meaning allows us to look at our Scheme-Prolog program as a logical specification of a problem for which the system is to find a solution)- is
where we intend (insert $x \ L0 \ L1$) to mean that inserti- L0 (at the right place) gives L1:	ng x into	 The operational meaning allows us to look at our Scheme-Prolog specification as an executable program for searching for a solution. 	:-
<pre>logic> (fact (insert ?a ?r (?a . ?r))) logic> (fact (insert ?a (?b . ?r) (?b . ?s)) (inser 1</pre>	rt ?a ?r ?s))	• Closed Universe Assumption: We make only positive statement: The closest we come to saying that something is false is to say the we can't prove it.	5. 1†
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- A plain, unbound logical variable will unify with anything. Must record this unification in the unifier we construct.
- Before unifying other (bound) logical variables, first must replace them with their recorded bindings, in order to make sure we bind consistently.
- To unify two atoms (numbers, booleans, symbols that are not logical variables), just compare them.
- To unify two lists: recursively unify their heads and tails.

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	Implementing Unific	cation: Code
ng. Must record	A simple tree recursion with side-effect	ts:
st must replace ke sure we bind	<pre>def unify(e, f, env): """Destructively extend ENV so as to o True if this succeeds and False other case (its existing bindings are never</pre>	unify (make equal) E and F, returning wise. ENV may be modified in either changed)."""
t are not logical	e = 100 kup(e, env) f = lookup(f, env)	
tails.	<pre>if scheme_eqvp(e, f): return True elif isvar(e): env.define(e, f) return True</pre>	
	elif isvar(f): env.define(f, e)	
	elif scheme_atomp(e) or scheme_atomp(: return False	f):
	else: return unify(e.first, f.first, en	<pre>v) and unify(e.second, f.second, env)</pre>
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Using Unification to Search for Proofs	
 The process of attempting to demonstrate an assertion (answer query) is a systematic depth-first search of facts. 	' a
<pre>def search(clauses, env): if clauses is nil: yield env for fact in fact database: fact = rename_variables(fact,) env_head = new environment that extends env if unify(conclusion of fact, first clause, env for env_rule in search(hypotheses of fact,</pre>	v_head): env_head): env_rule):
• In the actual program, we put on a <i>depth limit</i> : a limit on how deep the recursive calls on search may go.	oly
• This prevents us from going down infinite paths when there is finite path that will work.	۵
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