inst.eecs.berkeley.edu/~cs61c/su06

CS61C : Machine Structures

Lecture #21: Caches 2

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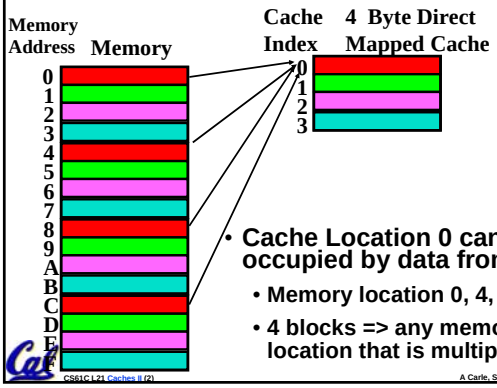
Review: Direct-Mapped Cache



- Cache Location 0 can be occupied by data from:
  - Memory location 0, 4, 8, ...
  - 4 blocks => any memory location that is multiple of 4

Issues with Direct-Mapped

Tag | Index | Offset

- Since multiple memory addresses map to same cache index, how do we tell which one is in there?
- What if we have a block size > 1 byte?
- Answer: divide memory address into three fields

	HEIGHT	WIDTH
tttttttttttttttt	iiiiiiiiii	oooo
tag to check if have correct block	index to select block	byte offset within block

Direct-Mapped Cache Terminology

- All fields are read as unsigned integers.
- Index: specifies the cache index (which "row" of the cache we should look in)
- Offset: once we've found correct block, specifies which byte within the block we want -- I.e., which "column"
- Tag: the remaining bits after offset and index are determined; these are used to distinguish between all the memory addresses that map to the same location

Direct-Mapped Cache Example (1/3)

- Suppose we have a 16KB of data in a direct-mapped cache with 4 word blocks
- Determine the size of the tag, index and offset fields if we're using a 32-bit architecture
- Offset
  - need to specify correct byte within a block
  - block contains 4 words
    - = 16 bytes
    - = 2^4 bytes
  - need 4 bits to specify correct byte

Direct-Mapped Cache Example (2/3)

- Index: (~index into an "array of blocks")
  - need to specify correct row in cache
  - cache contains 16 KB = 2^{14} bytes
  - block contains 2^4 bytes (4 words)
  - # blocks/cache
    - = $\frac{\text{bytes/cache}}{\text{bytes/block}}$
    - = $\frac{2^{14}\text{ bytes/cache}}{2^4\text{ bytes/block}}$
    - = 2^{10} blocks/cache
  - need 10 bits to specify this many rows

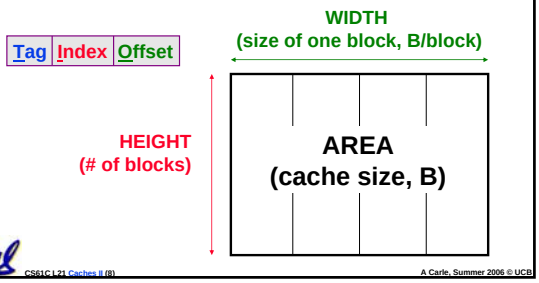
Direct-Mapped Cache Example (3/3)

- Tag: use remaining bits as tag
  - tag length = addr length - offset - index
    = 32 - 4 - 10 bits
    = 18 bits
  - so tag is leftmost 18 bits of memory address
- Why not full 32 bit address as tag?
  - All bytes within block need same address (4b)
  - Index must be same for every address within a block, so its redundant in tag check, thus can leave off to save memory (10 bits in this example)

TIO

AREA (cache size, B)
= HEIGHT (# of blocks)
* WIDTH (size of one block, B/block)

$2^{(H+W)} = 2^H * 2^W$



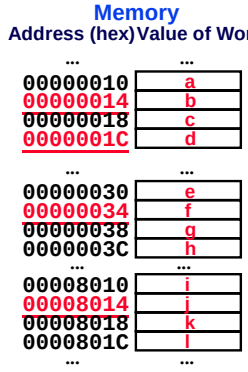
Caching Terminology

- When we try to read memory, 3 things can happen:

1. cache hit: cache block is valid and contains proper address, so read desired word
2. cache miss: nothing in cache in appropriate block, so fetch from memory
3. cache miss, block replacement: wrong data is in cache at appropriate block, so discard it and fetch desired data from memory (cache always copy)

Accessing data in a direct mapped cache

- Ex.: 16KB of data, direct-mapped, 4 word blocks
- Read 4 addresses
  1. 0x00000014
  2. 0x0000001C
  3. 0x00000034
  4. 0x00008014
- Memory values on right:
  - only cache/ memory level of hierarchy



Accessing data in a direct mapped cache

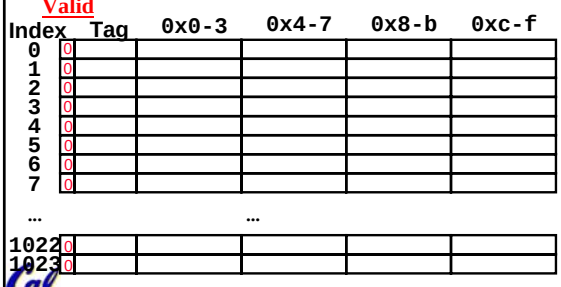
- 4 Addresses:
  - 0x00000014, 0x0000001C, 0x00000034, 0x00008014
- 4 Addresses divided (for convenience) into Tag, Index, Byte Offset fields

```
00000000000000000 0000000001 0100
00000000000000000 0000000001 1100
00000000000000000 0000000011 0100
00000000000000010 0000000001 0100
```

Tag Index Offset

16 KB Direct Mapped Cache, 16B blocks

- Valid bit: determines whether anything is stored in that row (when computer initially turned on, all entries invalid)



1. Read 0x00000014

- 00000000000000000000 0000000001 0100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	0					
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

So we read block 1 (0000000001)

- 00000000000000000000 0000000001 0100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	0					
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

No valid data

- 00000000000000000000 0000000001 0100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	0					
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

So load that data into cache, setting tag, valid

- 00000000000000000000 0000000001 0100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

Read from cache at offset, return word b

- 00000000000000000000 0000000001 0100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

2. Read 0x0000001C = 0…00 0..001 1100

- 00000000000000000000 0000000001 1100
  Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

Index is Valid

• 00000000000000000000 0000000001 1100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

Index valid, Tag Matches

• 00000000000000000000 0000000001 1100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

Index Valid, Tag Matches, return d

• 00000000000000000000 0000000001 1100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

3. Read 0x00000034 = 0…00 0..011 0100

• 00000000000000000000 0000000011 0100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

So read block 3

• 00000000000000000000 0000000011 0100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

No valid data

• 00000000000000000000 0000000011 0100

Tag field | Index field | Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	0					
4	0					
5	0					
6	0					
7	0					
...				...		
1022	0					
1023	0					

Load that cache block, return word f

• 00000000000000000 0000000011 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

4. Read 0x00008014 = 0…10 0..001 0100

• 00000000000000010 0000000001 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

So read Cache Block 1, Data is Valid

• 00000000000000010 0000000001 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

Cache Block 1 Tag does not match (0 != 2)

• 00000000000000010 0000000001 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	0	a	b	c	d
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

Miss, so replace block 1 with new data & tag

• 00000000000000010 0000000001 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	2	i	j	k	l
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

And return word j

• 00000000000000010 0000000001 0100
Tag field Index field Offset

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	2	i	j	k	l
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
…				…		
1022	0					
1023	0					

Peer Instruction #1

- Chose from: Cache: Hit, Miss, Miss w. replace
  Values returned: a ,b, c, d, e, ..., k, l
- Read address 0x00000030 ?
  00000000000000000 0000000011 0000
- Read address 0x0000001c ?
  00000000000000000 0000000001 1100

Cache

Index	Valid	Tag	0x0-3	0x4-7	0x8-b	0xc-f
0	0					
1	1	2	i	j	k	l
2	0					
3	1	0	e	f	g	h
4	0					
5	0					
6	0					
7	0					
...			...			

Answers

- 0x00000030 a hit
  Index = 3, Tag matches, Offset = 0, value = e
- 0x0000001c a miss
  Index = 1, Tag mismatch, so replace from memory, Offset = 0xc, value = d
- Since reads, values must = memory values whether or not cached:
  - 0x00000030 = e
  - 0x0000001c = d

Memory

Address	Value of Word
...	...
00000010	a
00000014	b
00000018	c
0000001c	d
...	...
00000030	e
00000034	f
00000038	g
0000003c	h
...	...
00008010	i
00008014	j
00008018	k
0000801c	l
...	...

Pre-Exam Exercise #2

We are now going to stop for ~5 minutes. During this time, your goal is to (by yourself) come up with a potential exam exercise covering the topic of Digital Logic, State Machines, or CPU Design. Make it as much like a real exam question as possible.

After this five minutes, you will explain your question to a small group and work through how you would go about solving it. I'll call on some random samples for the full class.

Administrivia

- HW6 Due Saturday
- Proj3 Due 8/8
- Midterm 2:
  - Friday, 11:00am – 2:00pm
  - 390 HMMB
  - Conflicts, DSP, &&|| terrified about the drop deadline: Contact Andy ASAP

Big Endian vs. Little Endian

Big-endian and little-endian derive from Jonathan Swift's *Gulliver's Travels* in which the Big Endians were a political faction that broke their eggs at the large end ("the primitive way") and rebelled against the Lilliputian King who required his subjects (the Little Endians) to break their eggs at the small end.

- The order in which BYTES are stored in memory
- Bits always stored as usual. (E.g., 0xC2=0b 1100 0010)

Consider the number 1025 as we normally write it:

BYTE3 BYTE2 BYTE1 BYTE0

00000000 00000000 00000100 00000001

Big Endian

ADDR3	ADDR2	ADDR1	ADDR0
BYTE0	BYTE1	BYTE2	BYTE3
00000001	00000100	00000000	00000000

ADDR0	ADDR1	ADDR2	ADDR3
BYTE3	BYTE2	BYTE1	BYTE0
00000000	00000000	00000100	00000001

Little Endian

ADDR3	ADDR2	ADDR1	ADDR0
BYTE3	BYTE2	BYTE1	BYTE0
00000000	00000000	00000100	00000001

ADDR0	ADDR1	ADDR2	ADDR3
BYTE0	BYTE1	BYTE2	BYTE3
00000001	00000100	00000000	00000000

www.webopedia.com/TERM/b/big_endian.html
searchnetworking.techtarget.com/sDefinition/0,,sid7_gci211659,00.html
www.noveltheory.com/TechPapers/endian.asp
en.wikipedia.org/wiki/Big_endian

Memorized this table yet?

- Blah blah Cache size 16KB blah blah 2^{23} blocks blah blah how many bits?
- Answer! 2^{XY} means…

X=0 ⇒ no suffix			Y=0 ⇒ 1
X=1 ⇒ kibi	~ Kilo	10^3	Y=1 ⇒ 2
X=2 ⇒ mebi	~ Mega	10^6	Y=2 ⇒ 4
X=3 ⇒ gibi	~ Giga	10^9	Y=3 ⇒ 8
X=4 ⇒ tebi	~ Tera	10^{12}	Y=4 ⇒ 16
X=5 ⇒ pebi	~ Peta	10^{15}	Y=5 ⇒ 32
X=6 ⇒ exbi	~ Exa	10^{18}	Y=6 ⇒ 64
X=7 ⇒ zebi	~ Zetta	10^{21}	Y=7 ⇒ 128
X=8 ⇒ yobi	~ Yotta	10^{24}	Y=8 ⇒ 256
			Y=9 ⇒ 512

How Much Information IS that?

www.sims.berkeley.edu/research/projects/how-much-info-2003/

- Print, film, magnetic, and optical storage media produced about 5 exabytes of new information in 2002. 92% of the new information stored on magnetic media, mostly in hard disks.
- Amt of new information stored on paper, film, magnetic, & optical media ~doubled in last 3 yrs
- Information flows through electronic channels -- telephone, radio, TV, and the Internet -- contained ~18 exabytes of new information in 2002, 3.5x more than is recorded in storage media. 98% of this total is the information sent & received in telephone calls - incl. voice & data on fixed lines & wireless.
  - WWW ⇒ 170 Tb of information on its surface; in volume 17x the size of the Lib. of Congress print collections.
  - *Instant messaging* ⇒ $5x10^9$ msgs/day (750GB), 274 TB/yr.
  - *Email* ⇒ ~400 PB of new information/year worldwide.

Block Size Tradeoff (1/3)

- Benefits of Larger Block Size
  - Spatial Locality: if we access a given word, we're likely to access other nearby words soon
  - Very applicable with Stored-Program Concept: if we execute a given instruction, it's likely that we'll execute the next few as well
  - Works nicely in sequential array accesses too

Block Size Tradeoff (2/3)

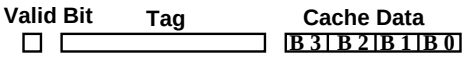
- Drawbacks of Larger Block Size
  - Larger block size means larger miss penalty
    - on a miss, takes longer time to load a new block from next level
  - If block size is too big relative to cache size, then there are too few blocks
    - Result: miss rate goes up
- In general, minimize Average Memory Access Time (AMAT)

  = Hit Time
  + Miss Penalty x Miss Rate

Block Size Tradeoff (3/3)

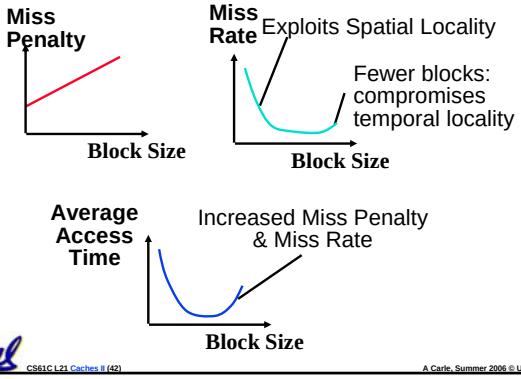
- Hit Time = time to find and retrieve data from current level cache
- Miss Penalty = average time to retrieve data on a current level miss (includes the possibility of misses on successive levels of memory hierarchy)
- Hit Rate = % of requests that are found in current level cache
- Miss Rate = 1 - Hit Rate

Extreme Example: One Big Block



- Cache Size = 4 bytes Block Size = 4 bytes
  - Only ONE entry in the cache!
- If item accessed, likely accessed again soon
  - But unlikely will be accessed again immediately!
- The next access will likely to be a miss again
  - Continually loading data into the cache but discard data (force out) before use it again
  - Nightmare for cache designer: Ping Pong Effect

Block Size Tradeoff Conclusions



Peer Instructions

1. All caches take advantage of spatial locality.
2. All caches take advantage of temporal locality.
3. On a read, the return value will depend on what is in the cache.

Peer Instruction Answer

1. All caches take advantage of spatial locality. FALSE
2. All caches take advantage of temporal locality. TRUE
3. On a read, the return value will depend on what is in the cache. FALSE

	ABC
1:	FFF
2:	FFT
3:	FTF
4:	FTT
5:	TFF
6:	TFT
7:	TTF
8:	TTT

1. Block size = 1, no spatial!
2. That's the idea of caches; We'll need it again soon.
3. It better not! If it's there, use it. Or, get from mem

And in Conclusion…

- Mechanism for transparent movement of data among levels of a storage hierarchy
  - set of address/value bindings
  - address ⇒ index to set of candidates
  - compare desired address with tag
  - service hit or miss
    - load new block and binding on miss